

Extra problem

The Ice Water Diet was a thing at one time. Drink water at 0°C and use energy from burning fat to raise the temperature to 37°C before releasing it. How much ice water would one need to drink to burn 140 calories (*i.e.*, what's in a can of Coke)?

First of all, when a dietician says 100 calories, that's dietary calories, each of which is equivalent to 4184 joules. Then,

$$Q = mc \Delta T \quad \rightarrow \quad m = \frac{Q}{c \Delta T} = \frac{4182 \frac{\text{J}}{\text{cal}} \times 140 \text{cal}}{4182 \frac{\text{J}}{\text{kg K}} \times (37 - 0)} = 3.78 \text{ kg} \sim 15 \text{ glasses} .$$

Then, FYI, to lose one pound of fat, you would need to drink

$$\begin{aligned} Q = mc \Delta T \quad \rightarrow \quad m &= \frac{Q}{c \Delta T} = \frac{4182 \frac{\text{J}}{\text{cal}} \times 3500 \text{cal}}{4182 \frac{\text{J}}{\text{kg K}} \times (37 - 0)} \\ &= 94.6 \text{ kg} \sim 378 \text{ glasses or 25 gallons of ice water} . \end{aligned}$$