HW 11-5 Soln)

For the simple pendulum:

$$P_{SP} = 2\pi \sqrt{\frac{L}{g}}$$

For the physical pendulum,

$$P_{PP} = 2\pi \sqrt{\frac{I}{Dgm}}$$

The moment of inertia of the sphere about the point of suspension can be found from the parallel axis theorem:

I = I_{CM} + mL² =
$$\frac{2}{5}$$
mR² + mL² = $\frac{2}{5}$ m(0.1L)² + mL² = 1.004 mL²

And of course D = L. So,

$$P_{PP} = 2\pi \sqrt{\frac{1.004 \text{ mL}^2}{\text{Lgm}}} = \frac{(1.002)2\pi \sqrt{\frac{1}{\text{gm}}}}{(1.002)2\pi \sqrt{\frac{1}{\text{gm}}}}$$

which is about a 0.2% difference.