PM-7 Soln)

Rewrite the expression as

$$\beta \; = \; \frac{1}{V} \frac{\Delta V}{\Delta T} \quad .$$

Since the pressure is constant, the ideal gas law tells us that

$$P \Delta V = nR\Delta T \rightarrow \frac{\Delta V}{\Delta T} = \frac{nR}{P}.$$

Then,

$$\beta \, = \, \frac{1}{V} \bigg( \frac{nR}{P} \bigg) = \, \frac{1}{T} \;\; .$$