

$$F_E = k_e \frac{q_1 q_2}{r^2} \quad k_e = \frac{1}{4\pi\epsilon_0}$$

$$\vec{F} = q\vec{E}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$dE = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2}$$

$$\Phi_E = \oint_{Surface} E_\perp dA = \frac{Q_{enclosed}}{\epsilon_0}$$

$$\Delta U = -q \int_a^b \vec{E} \cdot d\vec{r}$$

$$\Delta V = - \int_a^b \vec{E} \cdot d\vec{r}$$

$$\Delta V = (-) E \Delta x$$

$$V_{point\ charge} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$$

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r}$$

$$\vec{E} = -(\frac{\partial V}{\partial x} \hat{i} + \frac{\partial V}{\partial y} \hat{j} + \frac{\partial V}{\partial z} \hat{k}) = -\vec{\nabla}V$$

$$\vec{p} = q\vec{L}$$

$$\vec{\tau}_{Dipole} = \vec{p} \times \vec{E}$$

$$\tau_{Dipole} = p E \sin\theta_{p,E} (RHR)$$

$$U_{Dipole} = - \vec{p} \cdot \vec{E} = - p E \cos\theta_{p,E}$$

$$Q = CV$$

$$C = \frac{\kappa\epsilon_o A}{d}$$

$$U_C = \frac{Q^2}{2C} = \frac{1}{2} QV = \frac{1}{2} CV^2$$

$$\eta_E = \frac{1}{2} \epsilon_o E^2$$

$$C_{eq} = C_1 + C_2 + \dots$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots$$

$$I = \frac{dQ}{dt}$$

$$V = IR$$

$$R = \rho \frac{L}{A}$$

$$P = IV = I^2R = \frac{V^2}{R}$$

$$R_{eq} = R_1 + R_2 + \dots$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

$$\sum_n I_n = 0 ; \sum_n I_n R_n = \sum_n \epsilon_n$$

$$\vec{r} = \vec{r}_i + \vec{v}_i t + \frac{1}{2} \vec{a} t^2$$

$$\vec{v} = \vec{v}_i + \vec{a} t$$

$$v^2 = v_i^2 + 2 \vec{a} \cdot (\vec{r} - \vec{r}_i)$$

$$\vec{F}_{net} = \sum \vec{F}_n = m\vec{a}$$

$$\vec{F}_{grav} = \vec{g}m$$

$$\sum \vec{F}_{ext} = \frac{d\vec{p}}{dt}$$

$$F_x = - \frac{dU}{dx}$$

$$\sum \vec{\tau} = \frac{d\vec{L}}{dt}$$

$$\sum \vec{\tau} = I \vec{\alpha}$$

$$F_G = G \frac{m M}{r^2}$$

$$F_{fK} = \mu_K F_N \quad F_{fs} \leq \mu_s F_N$$

$$F_{Spring} = -kx$$

$$W_{NC} = \Delta K + \Delta U$$

$$K = \frac{1}{2} m v^2$$

$$U_{Grav} = gmy$$

$$U_{Spring} = \frac{1}{2} kx^2$$

$$U_{Electric} = qV$$

$$\vec{J}_{TOTAL} = \Delta \vec{p}$$

$$\vec{p} = m\vec{v}$$

$$\frac{d (e^{-ax})}{dx} = -ae^{-ax}$$

$$\int e^{-ax} = -\frac{e^{-ax}}{a}$$

$$\int \frac{dx}{x} = \ln x$$

$$\int \frac{dx}{x^2} = -\frac{1}{x}$$

$$\int \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 + x^2}}$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \arctan(\frac{x}{a})$$

$$\int \frac{dx}{\sqrt{a^2+x^2}} = \ln(2\sqrt{a^2+x^2}+2x)$$

$$\int \frac{x \ dx}{(a^2 + x^2)^{3/2}} = \frac{-1}{\sqrt{a^2 + x^2}}$$

$$\int \frac{x \ dx}{\sqrt{a^2 + x^2}} = \sqrt{a^2 + x^2}$$

$$\vec{C} = \vec{A} \times \vec{B} \Rightarrow C = AB \sin\theta_{A,B} \text{ (RHR)}$$

$$\vec{F} = q \vec{v} \times \vec{B} \quad F = qvB \sin\theta_{v,B} \text{ (RHR)}$$

$$\vec{F} = L \vec{I} \times \vec{B} \quad F = ILB \sin\theta_{I,B} \text{ (RHR)}$$

$$\vec{\mu} = NIA \text{ (RHR)}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B} \quad \tau = \mu B \sin\theta_{\mu,B} \text{ (RHR)}$$

$$U_{Dipole} = -\vec{\mu} \cdot \vec{B} = -\mu B \cos\theta_{\mu,B}$$

$$dB = \frac{\mu_0}{4\pi} \frac{dl}{r^2} I \sin\theta_{I,r} \text{ (RHR)}$$

$$\oint_{Surface} B_\perp dA = 0$$

$$\oint_{Loop} B_\parallel dl = \mu_0 I_{Enclosed}$$

$$B_{Center of Loop} = \frac{\mu_0 I}{2R}$$

$$B_{Wire} = \frac{\mu_0 I}{2\pi R}$$

$$B_{Solenoid} = \mu_0 nI$$

$$B_{Toroid} = \frac{\mu_0 NI}{2\pi r}$$

$$\Phi_m = \int B_\perp dA$$

$$\mathcal{E} = \oint_{Loop} \vec{E} \cdot d\vec{l} = (-)N \frac{d\Phi_m}{dt}$$

$$\mathcal{E}_L = (-)L \frac{dI}{dt}$$

$$\frac{V_P}{V_S} = \frac{N_P}{N_S}$$

$$U_L = \frac{1}{2}LI^2$$

$$\eta_B = \frac{B^2}{2\mu_0}$$

$$\tau_C = RC$$

$$Q(t) = CV_o e^{-t/RC}$$

$$V_C(t) = V_o e^{-t/RC}$$

$$I(t) = \frac{\mathcal{E}}{R} e^{-t/RC}$$

$$Q(t) = C\mathcal{E} (1 - e^{-t/RC})$$

$$V_C(t) = \mathcal{E} (1 - e^{-t/RC})$$

$$I(t) = (-) \frac{\mathcal{E}}{R} e^{-t/RC}$$

$$\tau_L = L/R$$

$$I(t) = \frac{\mathcal{E}}{R} (1 - e^{-Rt/L})$$

$$I(t) = \frac{\mathcal{E}}{R} e^{-Rt/L}$$

$$I_{rms} = \sqrt{(I^2)_{ave}}$$

$$I_{rms} = \frac{I_{max}}{\sqrt{2}} \text{ (sinusoidal)}$$

$$P_{av} = \frac{1}{2} \mathcal{E}_{max} I_{max} \cos\phi$$

$$P_{av} = I_{rms}^2 R = \frac{V_{R rms}^2}{R}$$

$$\begin{aligned}\frac{V_1}{V_2} &= \frac{N_1}{N_2} \\ \chi_L &= \omega L \\ \chi_C &= \frac{1}{\omega C} \\ \omega_0 &= \frac{1}{\sqrt{LC}} \\ \mathcal{E}_{\max} &= I_{\max} Z \\ Z &= \sqrt{R^2 + (\chi_L - \chi_C)^2} \\ \tan \phi &= \frac{\chi_L - \chi_C}{R} \\ \text{the } Q &= \frac{\omega_0}{\Delta \omega} = \frac{\omega_0 L}{R}\end{aligned}$$

$$\begin{aligned}\Phi_E &= \oint E_{\perp} dA = \frac{Q_{\text{enclosed}}}{\epsilon_o} \\ \Phi_M &= \oint B_{\perp} dA = 0 \\ \mathcal{E} &= \oint_{\text{Loop}} E_{\parallel} dl = - \frac{d\Phi_M}{dt} \\ \oint_{\text{Loop}} B_{\parallel} dl &= \mu_0 I + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} \\ \frac{\partial^2 \vec{E}}{\partial x^2} &= \frac{1}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} \\ \frac{\partial^2 \vec{B}}{\partial x^2} &= \frac{1}{c^2} \frac{\partial^2 \vec{B}}{\partial t^2} \\ c &= \frac{1}{\sqrt{\mu_0 \epsilon_0}} \\ E &= cB \\ \eta_{av} &= \frac{E_0 B_0}{2\mu_0 c}\end{aligned}$$

$$\begin{aligned}P &= \frac{F}{A} \\ P &= P_o + \rho gh \\ B &= \rho_{\text{Fluid}} g V_{\text{Displaced}} \\ \text{Rate} &= vA = \text{const} \\ \text{Rate} &= \frac{(P_1 - P_2) \pi r^4}{8L\eta} \\ P + \frac{1}{2} \rho v^2 + \rho gy &= \text{const} \\ \hline \hline \Delta L &= \alpha L_o \Delta T \\ \Delta V &= \beta V_o \Delta T \\ \beta &\approx 3\alpha \\ \hline \hline\end{aligned}$$

$$\begin{aligned}\frac{F}{A} &= Y \frac{\Delta L}{L_o} \\ \frac{F}{A} &= S \frac{\Delta x}{h} \\ \frac{F}{A} &= B \frac{\Delta V}{V_o}\end{aligned}$$

$$\begin{aligned}H &= \frac{k_{\text{Thermal}} A}{L} \Delta T \\ H &= e \sigma_{SB} A T^4 \\ \lambda_{\text{Peak}} &= \frac{0.003}{T}\end{aligned}$$

$$T_A = T_B = T_C$$

$$Q = \Delta U + W$$

$$\delta W = PdV$$

$$U_{AVE} = \gamma_2 k_B T_- (\text{for_each_type_of_motion})$$

$$Q_P = nc_{MP} \Delta T$$

$$Q_V = nc_{MV} \Delta T$$

$$Q = mL_F; Q = mL_V$$

for_gases:

$$PV = nRT$$

$$c_{MV} + R = c_{MP}$$

$$\gamma = \frac{c_{MP}}{c_{MV}}$$

$$PV = \text{const_}(isothermal)$$

$$PV^\gamma = \text{const_}(adiabatic)$$

$$TV^{\gamma-1} = \text{const_}(adiabatic)$$

for_solids:

$$c_{MP} \approx c_{MV}$$

$$dS = \frac{\delta Q}{T}$$

$$S = k_B \ln(g)$$