

1-5)

From above:

$$\mathbf{A} = 4\mathbf{i} + 3\mathbf{j} \quad \mathbf{B} = 5\mathbf{i} - 2\mathbf{j}$$

Use matrix method:

$i$	$j$	$k$	$i$	$j$
4	3	0	4	3
5	-2	0	5	-2

Multiply diagonally, positive down and to the right and negative down and to the left:

$$\mathbf{A} \times \mathbf{B} = 3*0*\mathbf{i} + 0*5*\mathbf{j} + 4*(-2)*\mathbf{k} - 4*0*\mathbf{j} - 0*(-2)*\mathbf{i} - 3*5*\mathbf{k} = (-8 -15)\mathbf{k} = -23\mathbf{k}, \text{ i.e., into the page.}$$

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Now, since  $\mathbf{A}$  and  $\mathbf{B}$  are in the x-y plane, it's fairly easy to use the other definition of the cross product as well:

$$|\mathbf{A}| = (4^2 + 3^2)^{1/2} = 5 \quad \text{and} \quad |\mathbf{B}| = (5^2 + (-2)^2)^{1/2} = 5.39$$

$$\theta_A = \arctan(3/4) = 36.9^\circ \quad \text{and} \quad \theta_B = \arctan(-2/5) = -21.8^\circ \quad (\text{Don't forget to check the quadrant!})$$

So, the angle between  $\mathbf{A}$  and  $\mathbf{B}$  is then  $58.7^\circ$ .

$$|\mathbf{A} \times \mathbf{B}| = |\mathbf{A}| |\mathbf{B}| \sin \theta_{A,B} = 5*5.39*\sin(58.7^\circ) = 23.0$$

and the RHR (with  $\mathbf{A}$  in QI and  $\mathbf{B}$  in QIII) gives us that the cross product points in the -z direction.

So, it checks!