

6-6)

$$m = 2\text{kg}, k = 400 \text{ N/m}, x_{\text{SPRING}i} = -0.22\text{m}, \theta = 37^\circ.$$

Use WE Theorem:

$W_N = 0$, since the normal force is always perpendicular to the path of the mass.

$W_g = \text{cons}$

$W_{\text{SP}} = \text{cons}$

So, $W_{\text{NC}} = 0$ and we have conservation of mechanical energy.

$$0 = K_f - K_i + U_{gf} - U_{gi} + U_{\text{SP}f} - U_{\text{SP}i}$$

a)

The initial situation is when the spring is compressed, the final situation is when the spring is relaxed and before the mass hits the incline.

$$\frac{1}{2}mv_i^2 + gmy_i + \frac{1}{2}k\chi_i^2 = \frac{1}{2}mv_f^2 + gmy_f + \frac{1}{2}k\chi_f^2$$

Here, y refers to altitude of the block above the plane at the bottom and χ refers to the compression of the spring, not to the location of the block in the horizontal direction. Some terms we realize are zero, in particular, v_i , y_i , y_f , and χ_f .

$$\frac{1}{2}k\chi_i^2 = \frac{1}{2}mv_f^2$$

So,

$$v_f = [k\chi_i^2/m]^{1/2} = [400*0.22^2/2]^{1/2} = 3.11 \text{ m/s}$$

b)

For (b), we can take the initial point to be when the spring is compressed, or the 'final' point from (a). I'll do the first, so that v_i , v_f , y_i , and χ_f are all zero:

$$\frac{1}{2}mv_i^2 + gmy_i + \frac{1}{2}k\chi_i^2 = \frac{1}{2}mv_f^2 + gmy_f + \frac{1}{2}k\chi_f^2$$

$$\frac{1}{2}k\chi_i^2 = gmy_f$$

$$y_f = k\chi_i^2/2mg = 400*0.22^2/2*2*9.8 = 0.49 \text{ m}$$

but, we want the distance up the incline, L :

$$y_f/L = \sin 37^\circ \rightarrow L = y_f/\sin 37^\circ = 0.49/0.6 = 0.82 \text{ m}$$