## 9-2)

## a)

Let the pivot point be the point of contact between the wheel and the kerb.

The angle theta will be given by  $\sin\theta = (R - h)/R$ 



We'll use lever arms for this one.  $\tau: \ 0^*F_{N2} + 0^*F_{fS} - F_A(R - h) - F_{N1}[R^2 - (R - h)^2]^{1/2} + gm[R^2 - (R - h)^2]^{1/2} = 0$ 

Now if the wheel just lifts off from the ground,  $F_{N1} \rightarrow 0$ . Solve for  $F_A$ :  $F_A = gm[R^2 - (R - h)^2]^{1/2}/(R - h) = gm[2Rh - h^2]^{1/2}/(R - h)$ 

Careful. This is the force necessary to just barely lift the wheel. Will it be enough to lift the wheel the whole way over the kerb? As the wheel rises, the lever arm of  $F_A$  increases, while the lever arm of gm decreases, so the wheel will actually accelerate up and over the kerb.

b) Now do for F<sub>B</sub> instead:  $\tau: 0*F_{N2} - F_B(2R - h) - F_{N1}[R^2 - (R - h)^2]^{1/2} + gm[R^2 - (R - h)^2]^{1/2} = 0$ Now if the wheel just lifts off from the ground,  $F_{N1} \rightarrow 0$ . Solve for F<sub>B</sub>:  $F_B = gm[R^2 - (R - h)^2]^{1/2}/(2R - h)$  $F_B = gm[2Rh - h^2]^{1/2}/(2R - h) = gmh^{1/2}[2R - h]^{1/2}/(2R - h) = gm[h/(2R - h)]^{1/2}$ 

Same argument as before; this is enough to just lift the wheel, and more than enough to lift it the whole way over the kerb.

c) Which force is larger?  $F_A/F_B = [gm[2Rh - h^2]^{1/2}/(R - h)]/[gm[h/(2R - h)]^{1/2}] = (2R - h)]/(R - h) >1; F_A > F_B$